

In this paper, we compare in one particular case, the arithmetic  $D$ -modules introduced by Berthelot and the arithmetic  $D$ -modules introduced by Mebkhout and Narvaez-Macarro. We prove that there exists an equivalence of categories of coherent  $D$ -modules when you consider the arithmetic  $D$ -modules introduced by Berthelot on a projective smooth formal scheme  $\mathcal{X}$ , over some discrete valuation ring  $R$  of mixed characteristics  $(0, p)$ , that is endowed with an ample divisor, along which the coefficients of the differential operators are overconvergent. On the side of Mebkhout-Narvaez-Macarro, you have to look at differential operators over a smooth, affine, weakly formal scheme over  $R$ , whose  $p$ -adic completion is the complementary of  $Z$  into  $\mathcal{X}$ . The equivalence of categories is given in one direction by taking global sections of the  $D$ -modules.